Motivation

- Radiative heat transfer is a key process in many combustion configurations, e.g., fire
- Accurate representation is challenging
 - Complex solution of the RTE
 - Complex representation of spectral gas and soot properties
 - Computationally expensive
 - Combustion simulation considers complex chemistry, turbulent flow, multicomponent mass transfer, soot formation
 - Burden on users/developers for submodel expertise
 - Availability of libraries that offload submodels facilitates code development and progress
 - Cantera, ...



https://energy.sandia.gov/programs/nuclearenergy/nuclear-energy-safety-security/



RADLIB

- RADLIB: radiative heat transfer library
- Provides radiative properties for use in RTE solvers
- Current models:
 - RCSLW
 - WSGG
 - Planck Mean
- Species: CO₂, H₂O, CO, soot
- Includes a 1D RTE solver
- Multiple examples
- Open source
- C++, Python, Fortran interfaces
- Published, documented





Models

• Spectral RTE (neglect scattering)

$$\frac{dI_{\eta}}{ds} = -\kappa_{\eta}I_{\eta} + \kappa_{\eta}I_{b,\eta}$$

- Absorption spectra include millions of spectral lines.
 - T, P, composition dependent
- Line-by-Line (LBL) solvers expensive, limited to simple configurations



https://commons.wikimedia.org/wiki/ File:Atmospheric_terahertz_transmittance_at_Mauna_Kea_(simul ated).svg



Global Models (WSGG)

- Spectrally integrated radiation properties
- Assume gray over wavenumber region j

$$\int_{\eta \in \{\Delta_j\}} \begin{pmatrix} \frac{dI_{\eta}}{ds} = -\kappa_{\eta}I_{\eta} + \kappa_{\eta}I_{b,\eta} \\ \frac{dI_{j}}{ds} = -\kappa_{j}I_{j} + a_{j}\kappa_{j}I_{b}, \quad j = 0, 1, \dots, n \end{cases}$$

$$a_j = \frac{\int_{\eta_j} I_{b,\eta} d\eta}{I_b} \qquad \sum_j a_j = 1$$

• Given spatial profiles of κ_j and a_j , solve for I_j profiles



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$$a_j = \frac{\int_{\eta_j} I_{b,\eta} d\eta}{I_b} \qquad \sum_j a_j = 1$$

Given spatial profiles of κ_j and a_j, solve for I_j profiles

• Total intensity

$$I = \int I_{\eta} d\eta = \sum_{j} I_{j}$$

• Heat flux (kW/m²)

$$\mathbf{q} = \int_{4\pi} I(\mathbf{s}) \mathbf{s} d\Omega$$

Volumetric heat source (kW/m³)

$$Q = -\nabla \cdot \mathbf{q}$$



- Integrating over wavenumber bands Δ_j is limited because κ_η varies widely within the band
- Spectral Line WSGG (SLW) models integrate over a set of (non-sequential) η for which the absorption cross section C_{η} is uniform (to within the C_{η} -width of the band)
 - $\kappa_\eta = C_\eta N$ where N is molar density
- κ_{j} just corresponds to the given band
- a_j is the fraction of the black emission in Δ_j

$$a_j = F(\tilde{C}_j; \phi, T) - F(\tilde{C}_{j-1}; \phi, T)$$
$$F(C; \phi, T) = \frac{1}{\sigma T^4} \int_{\{\eta: C_\eta(\eta, \phi) < C\}} E_b(\eta, T) d\eta$$

• F varies between 0 and 1 and is monotonic in C, so it can be inverted.



Solovjov et al. J. Quant. Spectrosc. Radiat. Tranf. 197:26-44 (2017)

WSGG



SLW



- The integrated RTE assumes Δ_j are independent of spatial position **x**, but C_η depends on the thermodynamic state ϕ , which depends on **x**.
- This is handled differently in variations of SLW models
- Rank correlation approach
 - Two positions with states ϕ_1 and ϕ_2 , with cross section spectra $C_{\eta}(\eta, \phi_1)$, $C_{\eta}(\eta, \phi_2)$
 - Let $\hat{C}_1 \equiv C_{\eta}(\hat{\eta}, \phi_1)$ and $\hat{C}_2 \equiv C_{\eta}(\hat{\eta}, \phi_2)$ denote the cross sections at some wavenumber $\hat{\eta}$
 - Define

$$H_1 = \eta : C_\eta(\eta, \phi_1) < \hat{C}_1$$
$$H_2 = \eta : C_\eta(\eta, \phi_2) < \hat{C}_2$$

• If $H_1=H_2$ for arbitrary $\hat{\eta}$ the spectra $C_{\eta}(\eta, \varphi_1)$, $C_{\eta}(\eta, \varphi_2)$ are rank correlated.

$$F(\hat{C}_{1}, \phi_{1}, T_{r}) = \frac{1}{\sigma T_{r}^{4}} \int_{H_{1}} E_{b}(\eta, T_{r}) d\eta$$

$$F(\hat{C}_{2}, \phi_{2}, T_{r}) = \frac{1}{\sigma T_{r}^{4}} \int_{H_{2}} E_{b}(\eta, T_{r}) d\eta$$

$$F(\hat{C}_{1}, \phi_{1}, T_{r}) = F(\hat{C}_{2}, \phi_{2}, T_{r})$$

• For a given state ϕ_1 and cross section \hat{C}_1 , we can evaluate F, then invert to find \hat{C}_2 at another ϕ_2

• Algorithm

- Specify a reference temperature T_r on the domain of interest (e.g. an average)
- Specify a collection of fixed F_j points with boundaries \tilde{F}_j (where 0<F<1)
- At each position with state ϕ invert F_j and \tilde{F}_j to compute C_j and \tilde{C}_j
- Compute the $\kappa_j = C_j N$ for each j at each position
- Compute the $a_j = F(\tilde{C}_j; \phi, T) F(\tilde{C}_{j-1}; \phi, T)$ for each j at each position



Algorithm

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- Compute the $a_j = F(\tilde{C}_j; \phi, T) F(\tilde{C}_{j-1}; \phi, T)$ for each j at each position
- ALBDF data is available:
 - H2O, CO2, and CO
 - P=0.1-50 atm,
 - T=300-3000 K.
 - Pearson et al. J. Quant. Spectrosc. Radiat. Transf. 143:83-91 (2018).
- For mixtures: $C_{\eta} = x_{CO_2}C_{CO_2,\eta} + x_{H_2O}C_{H_2O,\eta} + x_{CO}C_{CO,\eta}$

$$F_{\eta}(C_{\eta}) = F_{CO_{2},\eta}\left(\frac{C\eta}{x_{CO_{2}}}\right)F_{H_{2}O,\eta}\left(\frac{C\eta}{x_{H_{2}O}}\right)F_{CO,\eta}\left(\frac{C\eta}{x_{CO}}\right)$$

"multiplication method"



WSGG

WSGG model

- Bordbar et al., Combust. Flame, 161:2435-2445 (2014)
- Bordbar et al. Int. Commun. Heat Mass Transf., 110:104400 (2020)
- 4 gray + 1 clear gas
- H₂O, CO₂
- κ_j , a_j correlated to $M_r = x_{H2O}/x_{CO2}$,
 - 0.01 < Mr < 4 (interpolate to pure CO2, H2O outside)
- T = 300-2400 K
- Pressure-path length: 0.1-60 atm-m





PM

WSGG model

- Bordbar et al., Combust. Flame, 161:2435-2445 (2014)
- Bordbar et al. Int. Commun. Heat Mass Transf., 110:104400 (2020)
- 4 gray + 1 clear gas
- H₂O, CO₂
- κ_j , a_j correlated to $M_r = x_{H2O}/x_{CO2}$,
 - 0.01 < Mr < 4 (interpolate to pure CO2, H2O outside)
- T = 300-2400 K
- Pressure-path length: 0.1-60 atm-m

Planck Mean model

- TNF Workshop, https://tnfworkshop.org/radiation/
- H₂O, CO₂, CO, CH₄



• T = 300-2300 K





Soot

- Included in all three models
- Unagglomerated spheres
- Rayleigh small particle limit
- Neglects scattering
- Plank Mean:
 - κ_s is added to the κ_{gas}
- WSGG:
 - κ_s is added to each κ_j
- RCSLW
 - Spectral treatment
 - F_{s,η} computed and included in the mixture treatment (multiplication method)

$$\kappa_{s,\eta} = C_0 f_v \eta$$

$$\kappa_s = 3.72 \frac{f_v C_0 T}{C_2} = 1817 f_v T \ m^{-1}$$

$$C_0 = \frac{36\pi nk}{(n^2 - k^2 + 2)^2 + 4n^2 k^2}$$

$$C_2 = 0.014388 \ m \cdot K$$

- n, k are real, imaginary parts of the complex index of refraction
- n=1.75, k=1.03 \rightarrow C₀=7.03
 - Williams et al. Int. J. Heat Mass Transf. 50:1616-1630 (2007)



Examples

- 1D planar
- P = 1 atm, vary T, composition prof.
- 7 configurations
- Compare results with LBL simulations.
- Ray tracing: 1000 pts, 101 angles







- PM gives poor results
- WSGG is good except near walls
- RCSLW is nearly LBL

Examples

Example S5

- Black walls at 1500, 500 K
- Uniform $x_{H2O} = 0.1$
- Vary # Gray Gases







Examples

Example SB1

- Cold black walls
- Uniform T, composition
- T = 1000 K
- x_{H2O} = 0.2, x_{CO2} = 0.1





Publication

Computer Physics Communications 272 (2022) 108227



RadLib: A radiative property model library for CFD ☆,☆☆



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ARTICLE INFO

ABSTRACT

Article history: Received 3 January 2021 Received in revised form 25 October 2021 Accepted 7 November 2021 Available online 12 November 2021

Keywords: Radiative heat transfer Reacting flows CFD WSGG RCSLW RadLib is a C++ library of radiation property models that can be applied to variety of systems involving radiative heat transfer, including CFD simulations. RadLib includes three major radiation property models—Planck Mean (PM) absorption coefficients, the weighted sum of gray gases (WSGG) model, and the rank-correlation spectral line weighted-sum-of-gray-gases (RCSLW) model. RadLib includes C++, Python, and Fortran interfaces and can be expanded to include additional models. Several example cases illustrate use of the models with an included ray-tracing solver, compare their accuracy relative to line-by-line (LBL) solutions, and examine their computational costs. Additionally, an integrated CFD example of an ethylene burner configuration using Fire Dynamics Simulator (FDS) is provided. RadLib provides researchers with convenient access to validated radiation property models and a framework for further development.

Program summary

Program Title: RadLib

CPC Library link to program files: https://doi.org/10.17632/rs5kvnr86r.1 Developer's repository link: https://github.com/BYUignite/radlib Code Ocean capsule: https://codeocean.com/capsule/0997975/tree Licensing provisions: MIT

Programming language: C++, Fortran, Python

Nature of problem: Radiative heat transfer in combustion CFD problems is typically neglected or oversimplified, resulting in significant error and inaccuracy in combustion simulations. Radiation modeling, however, often requires a high degree of specialization due to its complexity and the challenges associated with implementation in existing CFD codes, which presents a substantial obstacle to researchers who wish to address the inaccuracies introduced by insufficient radiative heat transfer modeling in combustion simulations.

Solution method: We present RadLib, an open-source C++ library of validated radiation property models that can be applied alongside various RTE solution methods to ease some of the obstacles associated with radiation modeling for combustion CFD. The package includes C++, Fortran, and Python interfaces, several illustrative examples with a provided ray-tracing solver and an integrated example using Fire Dynamics Simulator (FDS). RadLib can also be expanded to include additional radiation property models and interfaces.

Additional comments including restrictions and unusual features: The library is intended to be used in Linuxlike terminal applications.



Github

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	David Lignell README.md on Feb 10			eb 10 🕑 125	Radiation property library for combustion gases and soot		
	data/rcslw_data cmake edits			9 months ago			
	docs	s Update Doxyfile: remove obsolete variables, 8 months ag				MIT License	
	examples	Update Doxyfile: remove obsolete	Update Doxyfile: remove obsolete variables, 8 months ago				
	src	Update Doxyfile: remove obsolete variables, 8 months ago			양 2 forks		
ß	.gitignore	Update .gitignore	te .gitignore 9 months ago				
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ß	LICENSE						
Ľ	README.md	DME.md README.md last month				Create a new release	
=	README.md				Packages No packages published Publish your first package		
F	Publication						
Т	This code is described in the following publication:				Contributors 2		
	V.B. Stephens, S. Jensen, I. Wheeler, D.O. Lignell, "RadLib: a radiative heat transfer model library for CFD," Computer Physics Communications, 272:108227, (2022).				vbstephens Victoria Stephens		
Д	A Code Ocean Capsule is also available.						
Д	A youtube video demonstrates building the code and running examples.				Environmente d		
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Code Ocean



 V_{VO}

YouTube





https://github.com/BYUignite/radlib



