## Excercise

- Write down the main topic/title of the last five classes on Python
- For each class, what were the main ideas
- Outline each class.
- Put in details
- What examples were done?
- Do this alone, then with your neighbor.
- Create your own review notes (like these slides).
- First "recall" then look up to fill in.


## Class 14: Variables, scope, tuples, dictionaries

- Variables tag objects
- $\mathrm{id}(\mathrm{x}) \rightarrow$ memory location of x
- type $(x) \rightarrow$ object type of $x$


## Variables, scope, tuples, dictionaries

## Ploting, numpy file i/o

## Modules and classes

## Integration



- Immutable objects: numbers, strings, tuples
- Mutable objects: lists, dictionaries, np arrays
- Scope, namespace
$\mathrm{g}=9.81$
$-\operatorname{def} f(m)$ :
return $\mathrm{m*}$ g \# use global $g$
$\mathrm{f}(10)$
98.10000000000001
def f(x):
def f(x):
x[2] = 55555
x[2] = 55555
x = [0,1,2]
x = [0,1,2]
f(x)
f(x)
print(x) \# x changed through func arg
print(x) \# x changed through func arg
[0, 1, 55555]
[0, 1, 55555]


## Class 14: Variables, scope, tuples, dictionaries

## Variables, scope, tuples, dictionaries

## Ploting, numpy file i/o

- Tuples
- Like lists, but immutable.
- Define as: $\mathrm{t}=(3.14,8314,101325,88)$
- Use comma for single element: $t=(3.14$,
- Unpacking: $x, y=(5,6)$
- Use to swap variables: $x=7, y=8 ; x, y=(y, x)$
- Access elements as $t[0]$, or $\mathrm{t}[\mathrm{i}]$, or $\mathrm{t}[i+5], \mathrm{t}[-1]$, etc.
- Dictionaries
- Like lists, but indexed by a key that we set, instead of indexed by integer
- Define as $t=\{k e y: v a l u e, ~ k e y: v a l u e, ~ e t c\}$.
- ages = \{'alice': 15, 'john': 88, 'bill': 22, 'sue': 19\}
- Access as ages['sue’]
- Functions: ages.keys(), ages.values(), ages.items()
- Functions: del ages['john'], ages.pop['john'], ages.popitem()
- Initialize: ages = \{\}
- Add data ages[some_key] = some_value


## Class 15:Plotting, file i/o



## Class 15:Plotting, file i/o

## Numpy

- np.savetxt
- np.loadtxt
- np.column_stack

Variables, scope, tuples, dictionaries
Ploting, numpy file i/o
Modules and classes
Integration

## Load from file

```
loaded_data = np.loadtxt("data.dat")
print(loaded_data)
```


## Create some data

```
x = np.linspace(0,10,25)
y_exp = x**0.6 + (np.random.rand(25) -0.5)
y_1 = x**0.6
y_2 = np.exp(-0.2*x)*np.cos(2*x)*2
```

Create a single 2-D array (matrix) for saving to a file

```
data = np.column_stack([x,y_exp, y_1, y_3])
print(data)
```


## Save to file

```
np.savetxt("data.dat", data, fmt='%10.5f', header="x, y_exp, y_1, y_2")
```


## Class 16: Modules, Classes

## import statement

- Import options for numpy:
import numpy as np
import numpy
import numpy as numnum
from numpy import sin, cos
from numpy import *
Ploting, numpy file i/o


## Modules and classes

- Modules


## Integration

- Save python code in a textfile as code.py
- Put in the same folder as you are using it from.
- Otherwise do this:
- Import sys
- Sys.path.append('path/to/folder/containing/the/module
- Import the modue: import code as c
- Use variables and functions:
- $x=c . s o m e \_v a r i a b l e$
- $y=$ c.some_function()


## Class 16: Modules, Classes

## - Classes

Variables, scope, tuples, dictionaries
Ploting, numpy file i/o

## Modules and classes

## Integration

```
class cube():
    def set_side(self, side):
    self.L = side
    def volume(self):
        return self.L**3
    def area(self):
        return 6 * self.L**2
```



## Class 17: Integration

## - Examples

- Simple numerical integration (rectangle)
- Sum of rectangle areas
- Trapazoid integration ( N trapazoids)

$$
I=-\frac{\Delta x}{2}\left(f_{0}+f_{N}\right)+\Delta x \sum_{i=0}^{N} f_{i}
$$

- Adaptive, recursive trapazoid integration
- Python quad function

```
from scipy.integrate import quad
def f(x, param):
    return x**2 + param
xlo = 1
xhi = 2
param = 3
I = quad(f, xlo, xhi, args=(param,))[0]
```


## Class 18: Solving Nonlinear Equations

- One equation and one unknown
- Put in $f(x)=0$ form.

```
import numpy as np
from scipy.optimize import fsolve
def f(x):
    return x**2 - 5
xg = 1
x = fsolve(f, xg)
```

- Add args if needed (as in quad)


## Class 18: Solving Nonlinear Equations

- Multiple equations in multiple unknowns
- Pass in an array of unknowns
- Return an array of equation values

```
import numpy as np
from scipy.optimize import fsolve
def hg(yz):
\begin{tabular}{ll}
\(\mathrm{y}=\mathrm{yz}[0]\) & \# recover the vars for convenience \\
\(\mathrm{z}=\mathrm{yz}[1]\) & \# compute the function values \\
\(\mathrm{h}=\mathrm{y}+2 * \mathrm{z}\) & \\
\(\mathrm{g}=\mathrm{np} \cdot \sin (\mathrm{y}) / \mathrm{z}\) & \\
return np.array([h, g]) \# return array of function values
\end{tabular}
```

\#---------------------------------------
yz_g = np.array([1,2])
$y z=f s o l v e\left(h g, y z \_g\right)$
$\mathrm{y}=\mathrm{yz}[0]$
$z=y z[1]$

- Note, use obvious names.
- Note the structure: recover, find equations, return array

